DISCUSSION FOR THIRD TUTORIAL

DATE: OCTOBER 24 OR 31, 2011 : DUE IN TUTORIAL NOVEMBER 7 OR 14, 2011

The following problem is called **Square Bashing** from Thinking Mathematically Second Edition p. 175.

Take any numbers satisfying a pattern of the form

$$4^2 + 5^2 + 6^2 = 2^2 + 3^2 + 8^2$$

Pair up the left and right numbers in any way at all, for example 42, 53, 68. Notice then that $42^2 + 52^2 + 62^2 - 24^2 + 25^2 + 86^2$

$$42^2 + 53^2 + 68^2 = 24^2 + 35^2 + 86^2$$

Why? Explain if such a manipulation will work for other types of pairings, when it will work and why.

Examples:

$$1^{2} + 4^{2} + 6^{2} + 7^{2} = 2^{2} + 3^{2} + 5^{2} + 8^{2}$$

$$1 + 4 + 6 + 7 = 2 + 3 + 5 + 8$$

$$3^{3} + 4^{3} + 5^{3} = 0^{3} + 0^{3} + 6^{3}$$