

MATH 2590 – Exercises on Digital Hearing Aids (Answers)

PART 1 ANSWERS

$$\begin{aligned}1. & 0.62 \\& = 0.62 \times 2 = 1.24 = 1 \\& = 0.24 \times 2 = 0.48 = 0 \\& = 0.48 \times 2 = 0.96 = 0 \\& = 0.96 \times 2 = 1.92 = 1 \\& = 0.92 \times 2 = 1.84 = 1 \\& = 0.84 \times 2 = 1.68 = 1 \\& = 0.68 \times 2 = 1.36 = 1 \\& 0.1001111\end{aligned}$$

$$\begin{aligned}2. & 0.58 \\& = 0.58 \times 2 = 1.16 = 1 \\& = 0.16 \times 2 = 0.32 = 0 \\& = 0.32 \times 2 = 0.64 = 0 \\& = 0.64 \times 2 = 1.28 = 1 \\& = 0.28 \times 2 = 0.56 = 0 \\& = 0.56 \times 2 = 1.12 = 1 \\& = 0.12 \times 2 = 0.24 = 0 \\& 0.1001010\end{aligned}$$

$$\begin{aligned}3. & 0.95 \\& = 0.95 \times 2 = 1.90 = 1 \\& = 0.90 \times 2 = 1.80 = 1 \\& = 0.80 \times 2 = 1.60 = 1 \\& = 0.60 \times 2 = 1.20 = 1 \\& = 0.20 \times 2 = 0.40 = 0 \\& = 0.40 \times 2 = 0.80 = 0 \\& = 0.80 \times 2 = 1.60 = 1 \\& 0.1111001\end{aligned}$$

PART II ANSWERS

1. **10011000**

$$\begin{array}{r}1001100 \\+ 1100101 \\ \hline 10110001\end{array}$$

2. **11100**

$$\begin{array}{r}1010 \\+ 1111 \\ \hline 11001\end{array}$$

3. **11100**

$$\begin{array}{r}0111 \\+ 1110 \\ \hline 10101\end{array}$$

*Numbers in red indicate what has been carried.

PART III ANSWERS

$$\begin{aligned}1. & 0.1100101 \\& = 1 \times 2^{-1} + 1 \times 2^{-2} + 0 \times 2^{-3} + 0 \times 2^{-4} + 1 \times 2^{-5} + 0 \times 2^{-6} \\& \quad + 1 \times 2^{-7} \\& = 0.5 + 0.25 + 0.03125 + 0.0078125 \\& = 0.7890625\end{aligned}$$

$$\begin{aligned}2. & 0.1001111 \\& = 1 \times 2^{-1} + 0 \times 2^{-2} + 0 \times 2^{-3} + 1 \times 2^{-4} + 1 \times 2^{-5} + 1 \times 2^{-6} \\& \quad + 1 \times 2^{-7} \\& = 0.5 + 0.0625 + 0.03125 + 0.015625 + \\& \quad 0.0078125 \\& = 0.6171875\end{aligned}$$

$$\begin{aligned}3. & 0.1111001 \\& = 1 \times 2^{-1} + 1 \times 2^{-2} + 1 \times 2^{-3} + 1 \times 2^{-4} + 0 \times 2^{-5} + 0 \times 2^{-6} \\& \quad + 1 \times 2^{-7} \\& = 0.5 + 0.25 + 0.125 + 0.0625 + 0.0078125 \\& = 0.9453125\end{aligned}$$