# SOME CONNECTIONS BETWEEN ALGEBRAIC EXPRESSIONS AND SEQUENCES : PART III 

## FEBRUARY 16, 2004

Use the formulas from the handout entitled (Some Connections between Algebraic Expressions and Sequences : Part II) and the techniques we learned in class to find the coefficients in the following generating functions.
(1) coefficient of $q^{8}$ in $2 q /(1-q)^{2}$
(2) coefficient of $q^{7}$ in $1 /(1+2 q)^{3}$
(3) coefficient of $q^{4}$ in $(1+2 q)^{3}$
(4) coefficient of $q^{7}$ in $\left(1-q^{3}\right)\left(1-q^{3}\right) /(1-q)^{2}$
(5) coefficient of $q^{10}$ in $2 /(1-q)^{3}$
(6) coefficient of $q^{6}$ in $3 /(1-2 q)$
(7) coefficient of $q^{3}$ in $(1+5 q)(1+q)^{3}$
(8) coefficient of $q^{7}$ in $2 q^{2} /(1-q)^{3}$
(9) coefficient of $q^{6}$ in $\left(q+q^{2}\right) /(1-q)^{3}$
(10) coefficient of $q^{20}$ in $\left(1-q^{2}\right)\left(1-q^{3}\right)\left(1-q^{4}\right) /(1-q)^{3}$

