

## DESIGN CONSIDERATIONS OF A CIPHER

There are ways of sending data so that is theoretically impossible to recover the message without knowing the key. Systems like this are rarely used because they are inconvenient. The key may only be used once and must be as long as the message that is being sent.

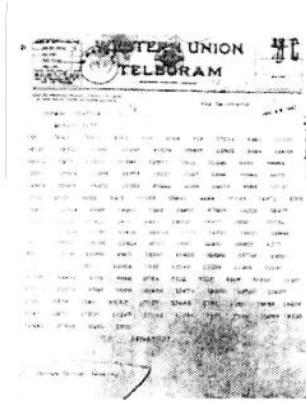
- Type of data (TV signal/voice/computer data/letter/telegram)
- Security
- Ease of Use
- Cost/ease of use vs. value of data
- Amount of data
- training of the people who do the encryption  
is simple (because they die frequently)

## Zimmermann Telegram

From Wikipedia, the free encyclopedia

The **Zimmermann Telegram** (or **Zimmermann Note**; German: *Zimmermann-Depesche*; Spanish: *Telegrama Zimmermann*) was a coded telegram dispatched by the Foreign Secretary of the German Empire, Arthur Zimmermann, on January 16, 1917, to the German ambassador in Mexico, Heinrich von Eckardt, at the height of World War I.

The telegram instructed the ambassador to approach the Mexican government with a proposal to form a military alliance against the United States. It promised Mexico land in the United States if they were to help. It was intercepted and decoded by the British, and its contents hastened the entry of the United States into World War I.



The Zimmermann telegram as it was sent from Washington to Mexico

Username:

4161user  
password:  
purple

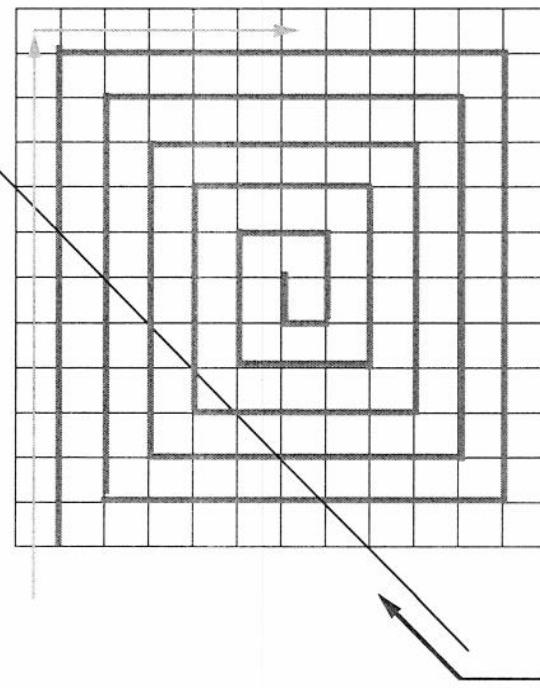
garsia.math.yorku.ca/~zabrocki/math4161w12/

$P=3$     $q=4$     $\# a \text{ key } OUT$

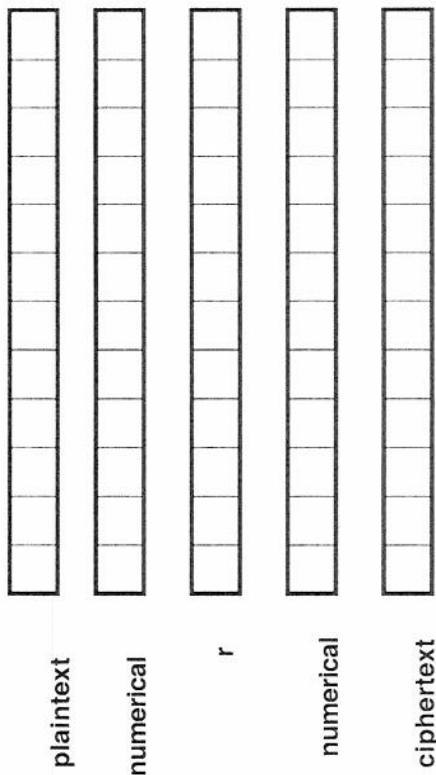
		VERNAME TWO-TAPE SYSTEM						
		O	U	L	T	O	U	T
a	14	20	19	14	20	19	14	20
D	R	O	P	D	R	O	P	D
b	3	17	14	15	3	17	14	15
r	17	11	7	3	23	10	2	9

## THE SNAIL ENCRYPTION SYSTEM

ENTER PLAINTEXT BY FOLLOWING THE SNAIL



READ BY DIAGONALS TO GET CIPHERTEXT  
DIRECTION OF READING



# Hill Encipherment

$$A = \begin{bmatrix} 1 & 2 \\ 1 & 5 \end{bmatrix} \quad A^{-1} = \begin{bmatrix} 5 & -2 \\ -1 & 11 \end{bmatrix} = \begin{bmatrix} 5 & 24 \\ 25 & 11 \end{bmatrix}$$

Key: a kxk matrix      k=2  
ALL ARITHMETIC IS DONE (MOD 26)

$$\det A = 11*5 - 2*1 = 53 \equiv 1 \pmod{26}$$

$$\begin{bmatrix} 1 & 2 \\ 1 & 5 \end{bmatrix} \begin{bmatrix} 5 & 24 \\ 25 & 11 \end{bmatrix} = \begin{bmatrix} 55+50 & 264+22 \\ 5+125 & 24+55 \end{bmatrix}$$

Plaintext: MEAT  
 Numerical: 12-4    0-19  
 $A^*$  plaintext:  
 Cyphertext:

Cyphertext: WU UO EI AY  
 Numerical: 22-20    20-14    4-8    0-24  
 $A^{-1}$  Cyphertext:  
 Plaintext:

# Playfair Cipher

Key		Plaintext		Ciphertext	
D	E	N	I	A	
L	B	C	F	G	
H	K	M	Q	P,	
Q	R	S	T	U,	
V	W	X	Y	Z	
H	I	J	K	L	
J	K	L	M	N	
L	M	N	O	P	
M	N	O	P	Q	
N	O	P	Q	R	
O	P	Q	R	S	
P	Q	R	S	T	
Q	R	S	T	U	
R	S	T	U	V	
S	T	U	V	W	
T	U	V	W	X	
U	V	W	X	Y	
V	W	X	Y	Z	
W	X	Y	Z		
X	Y	Z			
Y	Z				
Z					

### The Vigenere Square

A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z
B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A
C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B
D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C
E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D
F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E
G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F
H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G
I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H
J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I
K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J
L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K
M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L
N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M
O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N
P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O
Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P
R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q
S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R
T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S
U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T
V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U
W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V
X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W
Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X
Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y

A	0
B	1
C	2
D	3
E	4
F	5
G	6

A	7
B	8
C	9
D	10
E	11
F	12
G	13

### Caesar Cipher

B	R	E	A	T	H	O	F	R	E	S
I	T	R	E	A	T	H	O	F	R	E
L	N	O	P	Q	R	S	T	U	V	W
M	N	O	P	Q	R	S	T	U	V	W
N	O	P	Q	R	S	T	U	V	W	X
O	P	Q	R	S	T	U	V	W	X	Y
P	Q	R	S	T	U	V	W	X	Y	Z

### Vigenere Cipher

B	R	E	A	T	H	O	F	R	E	S
I	T	R	E	A	T	H	O	F	R	E
L	N	O	P	Q	R	S	T	U	V	W
M	N	O	P	Q	R	S	T	U	V	W
N	O	P	Q	R	S	T	U	V	W	X
O	P	Q	R	S	T	U	V	W	X	Y
P	Q	R	S	T	U	V	W	X	Y	Z

plaintext + key  
(mod 26)

ciphertext

Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O
R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P
S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q
T	U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R
U	V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S
V	W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T
W	X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U
X	Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V
Y	Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W
Z	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X

plaintext + key  
(mod 26)

ciphertext

$6 \times 4 \times$

$12 \times 2$

$3 \times 8$

$4 \times 6$

$8 \times 3$

$2 \times 12$

$24 \times 1$

$1 \times 24$


E	P	A	W
R			
F			

næse

N W E N  
A E P T  
S O R V  
E E D A  
R N L S  
E O Y N

N R O E L V  
A E E P Y A  
S W N R N S  
E E O D I N

## Homophonic Substitution

	A	B	C	D	E	F	G	H	I/J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z
S	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	1	2	3	4	5	6	7	8
T	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	1	2	3	4	5	6	7
A	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25
N	14	15	16	17	18	19	20	21	22	23	24	25	1	2	3	4	5	6	7	8	9	10	11	12	13

Key: STAN  
Plaintext #1: T H E N W H Y D I D Y O U T  
U R N S O M E O F U S I N S

# I D E O U T ?

ADFGVX

The ADFGVX system was first used in the battlefield march 5th 1918. Was broken June 1st by Georges Painvin

K<sub>2</sub>: A brief history of its use

K<sup>2</sup>: a permutation of N (even)

A	D	F	G	V	V
C	O	8	X	F	4
M	K	3	A	Z	9
N	W	L	O	J	D
S	I	Y	H	U	
P	1	V	B	6	R
E	Q	7	T	2	G

key  
fix

Key

Second

4	9	5	15	2	8	16	12	13	17	1	18	3	19	10	/	6	11	14	20
G	V	X	D	V	X	X	A	X	D	G	X	X	A			S	T	S	
H	Q	R	E	Q	U		E												
A	V	V	X	A	D	F	A	X	G	F	E	G	F			S	T	E	
F	R	O	N	T	L	I	N										B	Y	
G	F	X	G	G	X	D	G	X	G	G	F	A	D						
I	T	U	A	T	I	O	N												
X	G	X	A	F	F	X	A	X	V	X	D	G							
T	E	L	E	G	R	A	M	H	Q										
X	F	K	G	G	V	V	A	A	A	D	V	X	V	A					
7	T	H	C	O	R	P	S									E	S	D	

encrypted  
message

GFGVG VAGFG	XGADV	GAGXX	XXXXX	XXVGX
DAAAD XDXFV	VVFVF	GFFDG	GAGVA	AAGAA
XXXVA GGGXF	DGXAG	XFDXA	GGGVD	XFPXF
AFDGA	DDGDX			

69-16-9-2-85-33-81-35-51-25-61-40-13-1-45-93-85-20-64-77

A	D	F	G	V	X
F	L	U	B	E	R
N	T	S	A	C	D
G	H	I	J	K	M
Q	P	Q	V	W	X
Y	Z	Q	1	2	3
4	5	6	7	8	9
A	D	F	G	V	X

$$\begin{array}{r}
 3 \ 5 \ | \ 1 \ 7 \ | \ 9 \ 4 \ | \ 10 \ 2 \ | \ 8 \ 6 \\
 \hline
 A \ V \ | \ A \ P \ | \ L \ | \ F \ | \ I \ | \ L
 \end{array}$$