

## Practice

- (1) Below is a table of complex numbers, some in the form  $a + bi$  (rectangular coordinates) and the others in the form  $r(\cos\theta + i\sin\theta)$  (polar coordinates). Convert the ones in rectangular coordinates to polar and the reverse.

rectangular ( $a + bi$ )	polar $r(\cos\theta + i\sin\theta)$
$1 - i$	
$3 + 3i$	
$1 + \sqrt{3}i$	
	$3(\cos(\frac{4\pi}{3}) + i\sin(\frac{4\pi}{3}))$
	$\sqrt{2}(\cos(\frac{3\pi}{4}) + i\sin(\frac{3\pi}{4}))$
	$\cos(\frac{7\pi}{6}) + i\sin(\frac{7\pi}{6})$

- (2) Find all possible solutions to  $x^4 = -i$ .  
 (3) Find all possible solutions to  $x^3 = -\sqrt{3} + i$ .  
 (4) Prove that if  $a$  divides  $b$  and  $a$  divides  $c$  then  $a^2$  divides  $bc$ .  
 (5) Disprove that if  $a^2$  divides  $bc$ , then  $a$  divides  $b$  or  $a$  divides  $c$ .  
 (6) Prove that if  $2^2$  divides  $bc$ , then  $2$  divides  $b$  or  $2$  divides  $c$ .  
 (7) Prove that

$$\frac{1}{1 \cdot 2} + \frac{1}{2 \cdot 3} + \frac{1}{3 \cdot 4} + \cdots + \frac{1}{n(n+1)} = \frac{n}{n+1}$$