## Three sticks in a bag...

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Take three sticks which have their ends colored and place them in a bag. The first stick has two red ends, the second has two black ends and the third stick has a red and a black end.


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Now, reach into this bag (no peeking) and grasp one of the sticks by an end so that the other end is showing and pull the stick out. Say that a red end is showing.

What color is most likely clasped in your fist?


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Is the answer?
A) red
B) black
C) red/black are equally likely
D) don't know/care


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Looking at the wheel we see that $2 / 3$ of the time a red end will be hidden and $1 / 3$ of the time a black end will be hidden given that a red end is showing.


We are calculating the probability that a red or black is hidden GIVEN that a red is showing...

